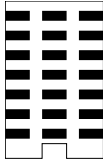


QUALITY FUNCTION DEPLOYMENT AND PROCESS MODELS

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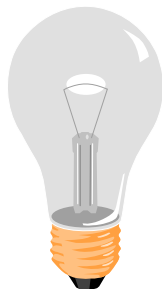
- INTRODUCTION
- DESIGN PROCESS
- RELATIONSHIP BETWEEN DESIGN PROCESS ATTRIBUTES AND VARIABLES
- OPTIMIZING THE QUALITY OF PERFORMING CRITICAL DESIGN ACTIVITIES
- SUMMARY



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What is Quality?



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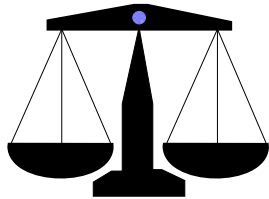
Quality is an abstract term,
often defined as
the extent to which the customers (users)
believe the product meets
their requirements and expectations



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Examples of Quality Measures



- General
Degree of customer satisfaction
- Specific
Reliability



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QFD - Basic Idea

Basic idea of QFD is to transform customer requirements into design requirements:

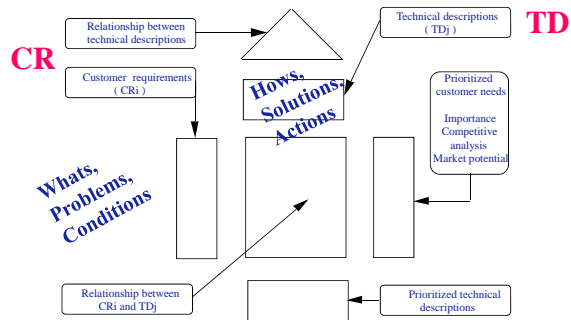
- QFD begins by obtaining the customer requirements (CRi) with respect to the product being designed
- Technical descriptions (DRj) are listed and evaluated from the point of view of the requirements



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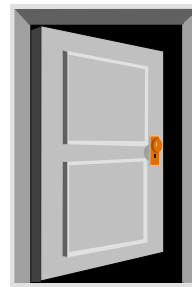
Quality Function Deployment (QFD) Matrix



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QFD



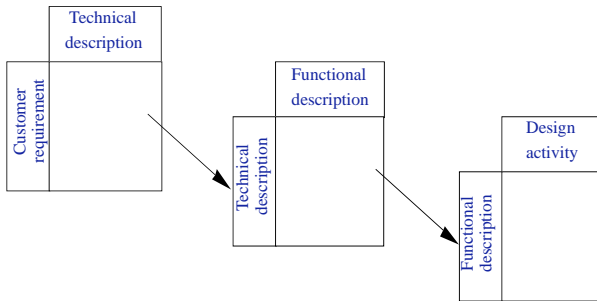
Known also as the House of Quality



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QFD Cascade



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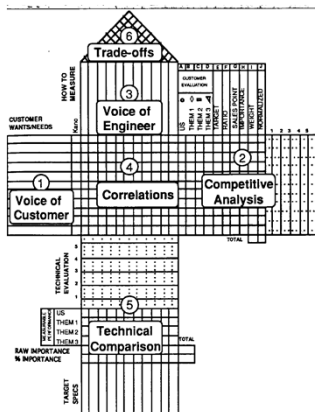
THE HOUSE OF QUALITY:

EXAMPLES



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Six steps
for building
a house
of quality



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Six step procedure for forming a QFD matrix

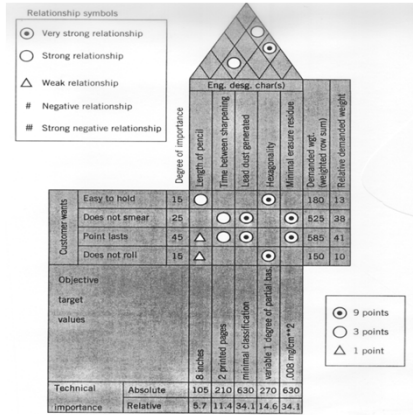
- Step 1. The primary customer requirements are normally expanded into secondary and tertiary requirements using AND/OR tree.
- Step 2. The design requirements must be related to the customer requirements and should be selectively deployed throughout the manufacturing, assembly, and service process to manifest themselves in the final product performance and customer acceptance.
- Step 3. Developing a matrix describing the customer requirements and the design requirements is accomplished
- Step 4. Market evaluation which covers the customer-expressed importance ratings, requirements, and competitive products is performed.
- Step 5. The target for each of the design requirement is defined.
- Step 6. Selection of the best solution should be deployed.



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Example 3



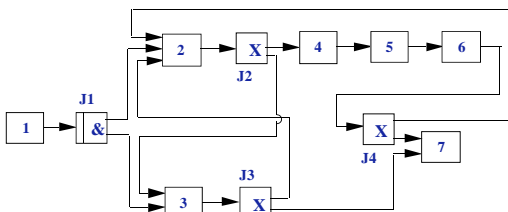
QFD Benefits

- Product objectives based on customer requirements are not misinterpreted at the subsequent stages
- Particular marketing strategies or sales points do not become lost or blurred during the translation process from marketing through planning to execution
- Important production control points are not overlooked - everything necessary to achieve the desired outcome is understood
- Efficiency is improved as the misinterpretation of design objectives, marketing perception, and critical control points, and the need for changes is minimized



DESIGN PROCESS

IDEF3 design process model of an electro-mechanical product



Activities

1. Prepare system specifications
2. Generate preliminary design
3. Evaluate cost of different alternatives
4. Build prototype
5. Perform tests on prototype
6. Analyze test data
7. Finalize design details



Modeling

RELATIONSHIP BETWEEN DESIGN PROCESS ATTRIBUTES AND VARIABLES OF CRITICAL ACTIVITIES

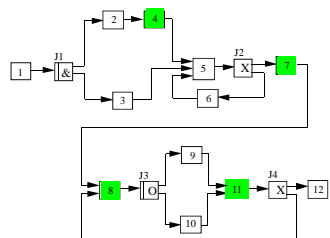
- An attribute is an element of a design process performance measure or the measure itself
- An attribute is a function of design process variables



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Process model with critical activities



Modeling attribute-variable relationship

■ Critical activity



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List of activities of the design process

No.	Activity
1	Perform project planning
2	Review and analyze customer requirements
3	Develop project coordination document
4	Define design requirements
5	Establish system design goals
6	Perform system tradeoffs
7	Finalize product requirements
8	Develop system requirements
9	Conduct internal requirements review
10	Review requirements with customer
11	Analyze modifications of system specifications
12	Finalize the system specifications



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QFD in Design



Relationships

(a) Process attribute - process variable

(b) Activity - attribute

(c) Other relationships



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Symbols used in the house of quality for design process attributes and variables

Relationship Matrix	
●	Strong positive
○	Medium positive
▽	Weak positive
×	Negative

Interaction Matrix	
○	Positive
×	Negative



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House of quality for a design process

Design Process Attributes	Design Process Variables			
	Average resource level savings	No. of design projects undertaken	Frequency of interaction among different design functional groups	No. of supporting functional groups involved
No. of design activities delayed due to the resources being not available	●	○		●
Risk of violating the due date	○	●	○	
Average lateness of design activities	○	●		▽
Completion time of the last design activity in the network	○	○	●	▽



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Conversion of symbols

Symbol	Coefficient Value
●	+9
○	+3
▽	+1
×	-3

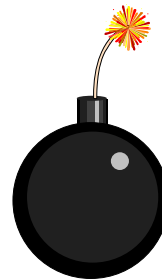
Design Process Attributes	Design Process Variables			
	Average resource level savings	No. of design projects undertaken	Frequency of interaction among different design functional groups	No. of supporting functional groups involved
No. of design activities delayed due to the resources being not available	●	○		●
Risk of violating the due date	○	●	○	
Average lateness of design activities	○	●		▽
Completion time of the last design activity in the network	○	○	●	▽



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Relationships Quantification



Converting QFD into a mathematical programming model



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The Design Process Example

Relationships

Attribute - variable

or

Activity - attribute (characteristic)



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Design process attributes

$y = (y_1, \dots, y_i, \dots, y_n)$

Feasible range for y_i is:

$y_{iL} \leq y_i \leq y_{iU}$

Design process attributes
and their feasible ranges

	Attribute	Range
y_1	No. of design activities delayed due to the resources not being available	$0 \leq y_1 \leq 8$
y_2	Risk of violating the due date	$0 \leq y_2 \leq 1$
y_3	Average lateness of design activities	$2.5 \leq y_3 \leq 9.4$
y_4	Completion time of the last design activity in the network	$18 \leq y_4 \leq 35$



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Values of the design process variables:

$x = (x_1, \dots, x_i, \dots, x_m)$

Feasible range for x_i is:

$x_{iL} \leq x_i \leq x_{iU}$

Design Process Variables and their Feasible Ranges

Variable	Range
Average resource level savings	$3.2 \leq x_1 \leq 8.4$
Number of design projects undertaken	$4 \leq x_2 \leq 10$
Frequency of interaction among different design functional groups	$2 \leq x_3 \leq 6$
Number of supporting functional groups involved	$5 \leq x_4 \leq 10$



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Attribute y_i is a function of the design process variables

$$y_i = f(x)$$

The design process variables are scaled in the range of 0 to 1 to obtain the vector of relative design process variable values:

$$x' = (x_1', x_2', \dots, x_m')$$

$$y_i' = f(x')$$



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Why scaling variables?



Same 'weight' assigned to each variable



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For x's scaled in [0, 1]

$$y_1' = 9x_1' + 3x_2' + 9x_4' + 3x_1'x_2' - 3x_1'x_4'$$

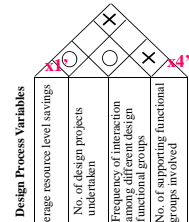
$$y_2' = 3x_1' + 9x_2' + 3x_3' + 3x_1'x_2' + 3x_2'x_3'$$

$$y_3' = 3x_1' + 9x_2' + x_4' + 3x_1'x_2' - 3x_1'x_4'$$

$$y_4' = 3x_1' + 3x_2' + 9x_3' + x_4' + 3x_1'x_2' + 3x_2'x_3' - 3x_1'x_4' - 3x_3'x_4'$$

Symbol	Coefficient Value
●	+9
○	+3
▽	+1
×	-3

	Design Process Attributes			
	No. of design activities delayed due to the resources being not available	Risk of violating the due date	Average lateness of design activities	Completion time of the last design activity in the network
y_1'	●	○	○	●
y_2'	○	●	○	▽
y_3'	○	○	○	●
y_4'	○	○	●	▽



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Scaling equations

Consider equation y_2' :

$$y_2' = 3x_1' + 9x_2' + 3x_3' + 3x_1'x_2' + 3x_2'x_3'$$

$$\min y_2' = 0 \text{ and } \max y_2' = 21$$

Note: (21 - 0) is the range for y_2' obtained by maximizing and minimizing

$$y_2' = 3x_1' + 9x_2' + 3x_3' + 3x_1'x_2' + 3x_2'x_3'$$

and (1 - 0) the range for y_2 from the table

Expression for y_2 as a function of x's scaled in [0, 1]:

$$y_2 = 0 + (1 - 0) (3x_1' + 9x_2' + 3x_3' + 3x_1'x_2' + 3x_2'x_3') / (21 - 0)$$

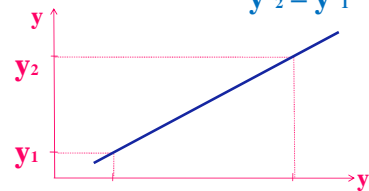


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Equation Balancing

$$y - y_1 = \frac{y_2 - y_1}{y_2' - y_1'} (y' - y_1')$$



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Balancing equation

Shifting by lower y limit

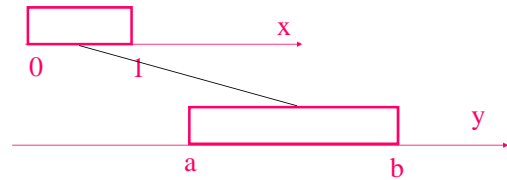
$$y = \text{Lower limit of } y + (\text{y range})[y' / (\text{y}' \text{ range})]$$

Scaling to y range Scaling of y' to $[0, 1]$

Example $y^2 = 0 + (1 - 0) y^{2'} / (21 - 0)$



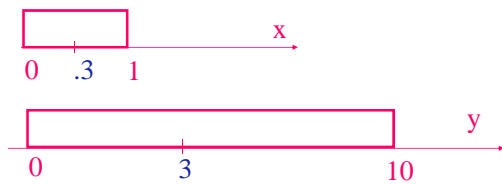
Scaling



$$y = a + (b - a)x$$



Example 1

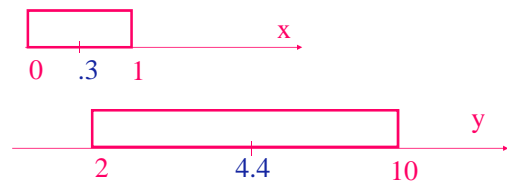


$$y = a + (b - a)x$$

$$y = 0 + (10 - 0)x = 1x, 3 = 3$$



Example 2



$$y = a + (b - a)x$$

$$y = 2 + (10 - 2)x = 2 + 8x, 3 = 4.4$$



Expression for y_s as a function of x 's scaled in $[0, 1]$:
(ranges determined using Lingo Optimization Software)

$$y_1 = 0 + (8 - 0)(9x_1' + 3x_2' + 9x_4' + 3x_1'x_2' - 3x_1'x_4' + 3x_2'x_4') / (24 - 0)$$

$$y_2 = 0 + (1 - 0)(3x_1' + 9x_2' + 3x_3' + 3x_1'x_2' + 3x_2'x_3') / (21 - 0)$$

$$y_3 = 2.5 + (9.4 - 2.5)(3x_1' + 9x_2' + x_4' + 3x_1'x_2' - 3x_1'x_4') / (15 - 0)$$

$$y_4 = 18 + (35 - 18)(3x_1' + 3x_2' + 9x_3' + x_4' + 3x_1'x_2' + 3x_2'x_3' - 3x_1'x_4' - 3x_3'x_4') / (21 - 0)$$



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EXAMPLE 4: Critical design activities used as design process attributes and their feasible ranges

	Activity No.	Critical Activity Name	Limits
y_1	4	Define design requirements	$0 \leq y_1 \leq 1$
y_2	7	Finalize product requirements	$0 \leq y_2 \leq 1$
y_3	8	Develop system requirements	$0 \leq y_3 \leq 1$
y_4	11	Analyze modifications of system specifications	$0 \leq y_4 \leq 1$



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Variables affecting the quality of design activities and their limits

Variable	Limits
x_1 Average level of expertise	$0 \leq x_1 \leq 8$
x_2 Average resource level	$4.6 \leq x_2 \leq 12.34$
x_3 Frequency of interaction between different functional design groups	$1 \leq x_3 \leq 5$
x_4 Number of resource preemptions	$8 \leq x_4 \leq 25$
x_5 Number of information sources	$3 \leq x_5 \leq 11$



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House of quality for relationships between critical activities and process variables

Critical Design Activities	Design Process Variables			
	Average level of expertise	Average resource level	Frequency of interaction among different functional groups	Number of resource preemptions
Define derived requirements	○	▽	×	●
Finalize product requirements	●	○	○	▽
Develop system requirements specifications	●	▽	●	○
Analyze modifications suggested in system specifications	○	●	○	×



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$$y_1 = 0 + (1 - 0)(3x_1' + x_2' - x_4' + 9x_5' - x_1'x_2' - x_1'x_5' + 3x_2'x_4') / (13 - (-1))$$

$$y_2 = 0 + (1 - 0)(9x_1' + 3x_3' + x_5' - x_1'x_5' + 3x_3'x_5') / (15 - 0)$$

$$y_3 = 0 + (1 - 0)(9x_1' + x_2' + 9x_3' + 3x_5' - x_1'x_2' - x_1'x_5' + 3x_3'x_5') / (23 - 0)$$

$$y_4 = 0 + (1 - 0)(3x_1' + 9x_2' + 3x_3' - x_4' - x_1'x_2' + 3x_2'x_4') / (16 - (-1))$$



Maximize $w_1y_1 + w_2y_2 + w_3y_3 + w_4y_4$

s.t.

$$y_1 = 0 + (1 - 0)(3x_1' + x_2' - x_4' + 9x_5' - x_1'x_2' - x_1'x_5' + 3x_2'x_4') / 14$$

$$y_2 = 0 + (1 - 0)(9x_1' + 3x_3' + x_5' - x_1'x_5' + 3x_3'x_5') / 15$$

$$y_3 = 0 + (1 - 0)(9x_1' + x_2' + 9x_3' + 3x_5' - x_1'x_2' - x_1'x_5' + 3x_3'x_5') / 23$$

$$y_4 = 0 + (1 - 0)(3x_1' + 9x_2' + 3x_3' - x_4' - x_1'x_2' + 3x_2'x_4') / 17$$

$$0 \leq x'_i \leq 1 \quad \text{for } i = 1, 2, 3, 4, 5$$



Example

$$w_1 = 10, \quad w_2 = 35, \quad w_3 = 20, \quad w_4 = 15$$

Maximize $10y_1 + 35y_2 + 20y_3 + 15y_4$

s.t.

$$y_1 = 0 + (1 - 0)(3x_1' + x_2' - x_4' + 9x_5' - x_1'x_2' - x_1'x_5' + 3x_2'x_4') / 14$$

$$y_2 = 0 + (1 - 0)(9x_1' + 3x_3' + x_5' - x_1'x_5' + 3x_3'x_5') / 15$$

$$y_3 = 0 + (1 - 0)(9x_1' + x_2' + 9x_3' + 3x_5' - x_1'x_2' - x_1'x_5' + 3x_3'x_5') / 23$$

$$y_4 = 0 + (1 - 0)(3x_1' + 9x_2' + 3x_3' - x_4' - x_1'x_2' + 3x_2'x_4') / 17$$

$$0 \leq x'_i \leq 1 \quad \text{for } i = 1, 2, 3, 4, 5$$



Max $33.62x_1' + 10.58x_2' + 17.47x_3' - 1.60x_4' + 11.37x_5' - 2.47x_1'x_2' - 3.92x_1'x_5' + 4.79x_2'x_4' + 9.61x_2'x_5'$

s.t.

$$0 \leq x'_i \leq 1 \quad \text{for } i = 1, 2, 3, 4, 5$$

The optimal solution (scaled in [0, 1]) is:

$$x_1' = 1.00, \quad x_2' = 1.00, \quad x_3' = 1.00, \\ x_4' = 1.00, \quad x_5' = 1.00$$



Objective Function:

$$\text{Max} = 100((1/18)(0.74x_1 + x_2 - 0.9x_3 + 0.7x_4 - x_5) - x_1^2 - x_2^2 - x_3^2 - x_4^2 + 3x_5^2) + 35((1/15)(0.74x_1 + 3x_2) + x_3 - x_4 - x_5) - x_1^2 - x_2^2 - x_3^2 - x_4^2 + 3x_5^2$$

$$+ 20((1/25)(0.74x_1 + x_2 + 0.9x_3 + 3x_4 - x_5) - x_1^2 - x_2^2 - x_3^2 - x_4^2 + 3x_5^2) + 15((1/17)(0.74x_1 + 3x_2) + x_3 - x_4 - x_5) - x_1^2 - x_2^2 - x_3^2 - x_4^2 + 3x_5^2$$

Subject to Constraints:

Non-negativity Constraints:

$$0 \leq x_1$$

$$0 \leq x_2$$

$$0 \leq x_3$$

$$0 \leq x_4$$

$$1 \leq x_5$$

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Global optimal solution found.

Objective value: 76.40336

Expanded solver usage: 1

Total solver iterations: 41

Variable	Value	Reduced Cost
X1P	1.000000	0.000000
X2P	1.000000	0.000000
X3P	1.000000	0.000000
X4P	1.000000	0.000000
X5P	1.000000	0.000000

Row	Status or Surplus	Dual Price
1	76.40336	1.000000
2	1.000000	0.000000
3	1.000000	0.000000
4	1.000000	0.000000
5	1.000000	0.000000
6	1.000000	0.000000
7	0.000000	-27.13211
8	0.000000	-11.84874
9	0.000000	-27.08184
10	0.000000	-3.192777
11	0.000000	-17.06211

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Variable	Limits
x1	Average level of expertise $0 \leq x_1 \leq 8$
x2	Average resource level $4.6 \leq x_2 \leq 12.34$
x3	Frequency of interaction between different functional design groups $1 \leq x_3 \leq 5$
x4	Number of resource preemptions $8 \leq x_4 \leq 25$
x5	Number of information sources $3 \leq x_5 \leq 11$

$x_1' = 1.00, \quad x_2' = 1.00, \quad x_3' = 1.00,$
 $x_4' = 1.00, \quad x_5' = 1.00$

E.g., $x_1 = 0 + (8 - 0)x_1' = 8$
 $x_2 = 4.6 + (12.34 - 4.6)x_2' = 12.34$

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Values of variables affecting the quality of critical design activities

Variable	Best Value	Alternative Value
x1	6	6
x2	11	9
x3	4	4
x4	10	10
x5	9	7
Value of the Objective Function	68.1	59.33

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